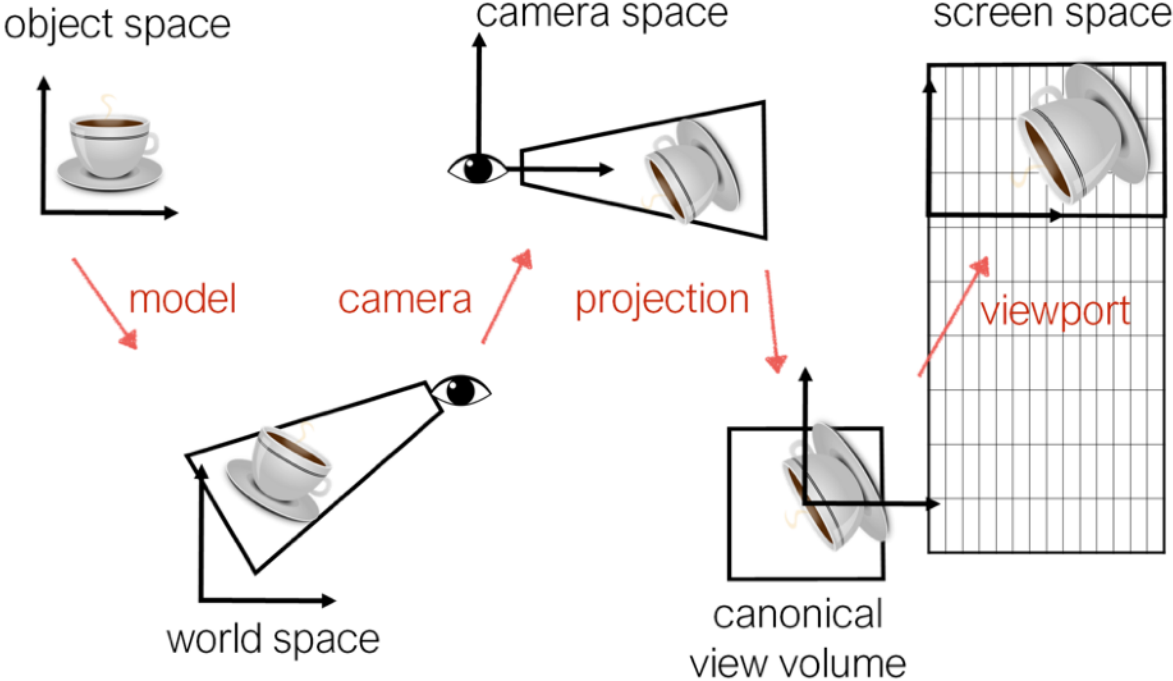


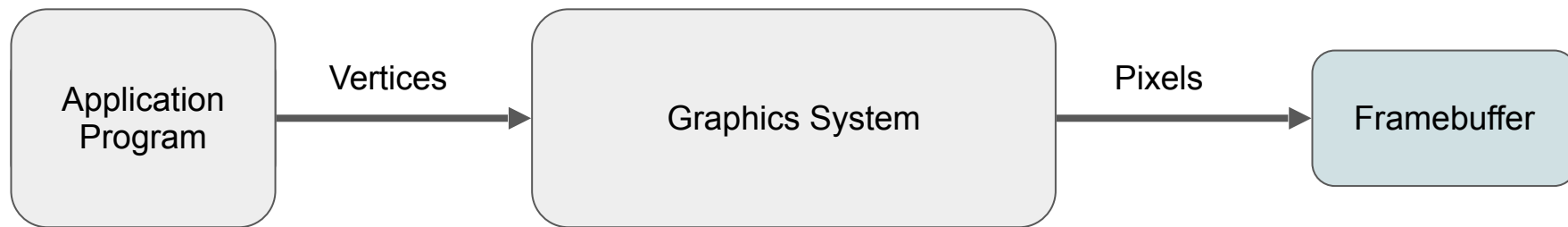
# Rendering Pipeline 1

CS 425: Computer Graphics 1

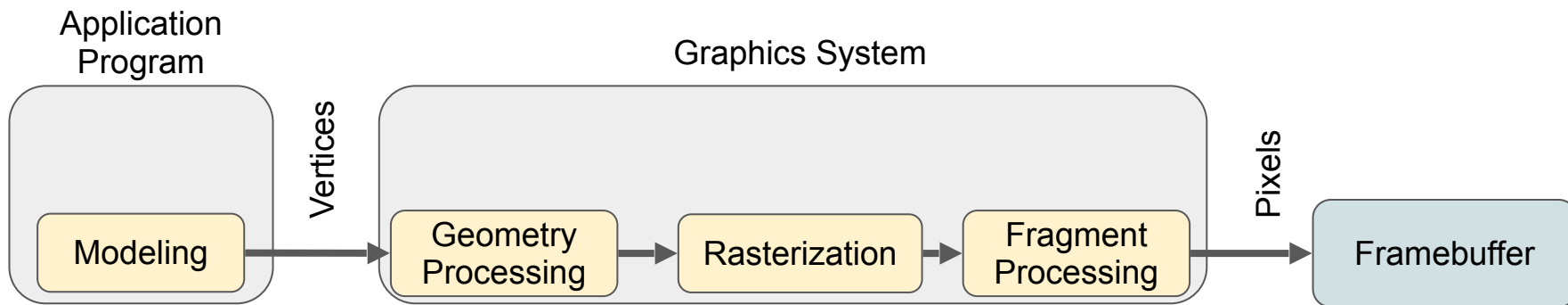
# Recap: Transformations



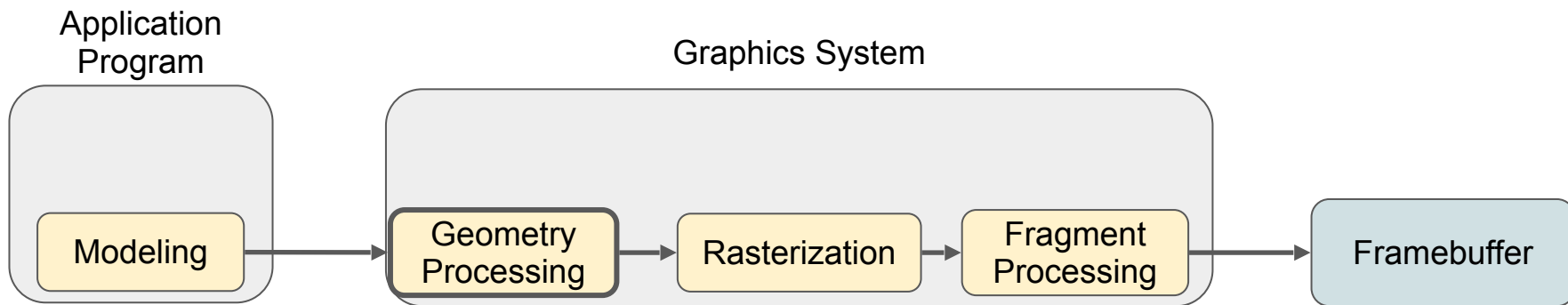
# Graphics System



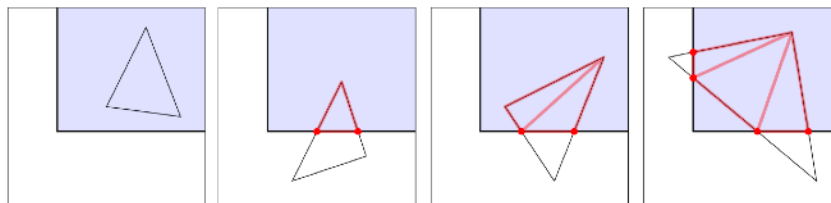
# Graphics Pipeline



# Clipping



## Clipping



From: <https://paroj.github.io/gltut/>

# Geometry Processing

- View transformations
- Projection
- Primitive assembly
- **Clipping**
- Shading

# Geometry Processing

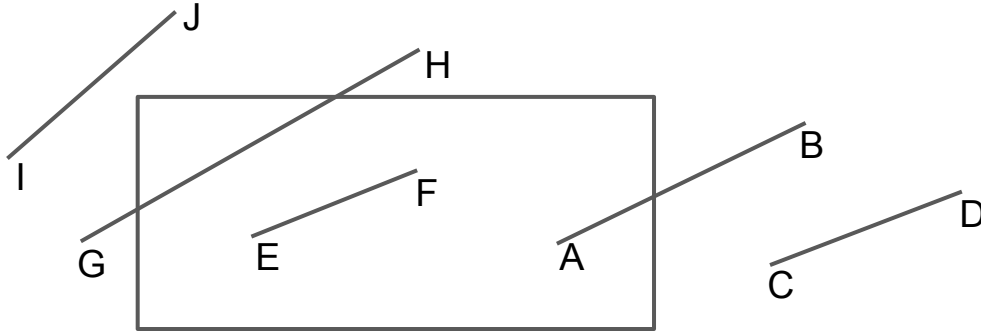
- **Projection:**
  - Transforming to a normalized view volume.
  - View volume will be a cube of size 2, centered at origin.
  - Eliminates dependency on application specifications as well as display device specifications.
- **Primitive Assembly:**
  - Grouping of vertices to form objects (primitives).
  - Done before clipping.
- **Clipping**
- **Shading**
  - Assignment of colors to vertices and determining how the intermediate vertices are to be colored.

# Why clipping?

- Rasterization is expensive.
  - Optimize what needs to be rasterized.
  - Clipping: removes geometry and primitives that will not appear on the screen
- Brute force approach: Clip every primitive against all the four sides of the view window (or six sides of the view volume)
- Computing intersections can be expensive since these calculations involve floating point divisions.

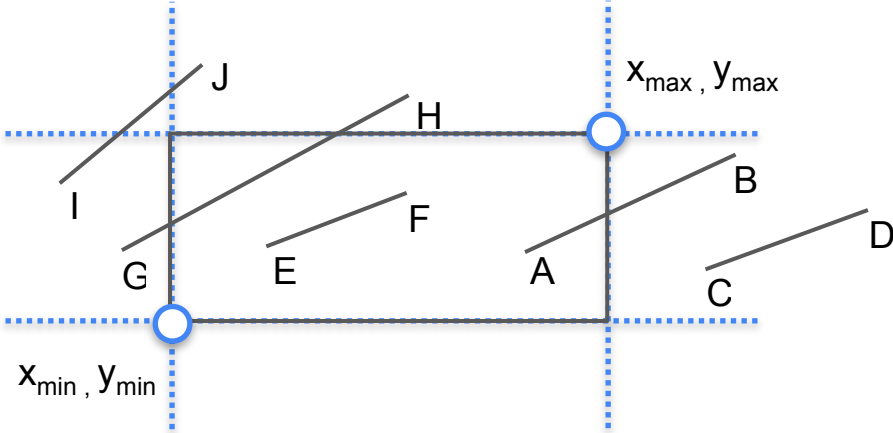
# Clipping: Line segments

## Cohen-Sutherland Line Clipping



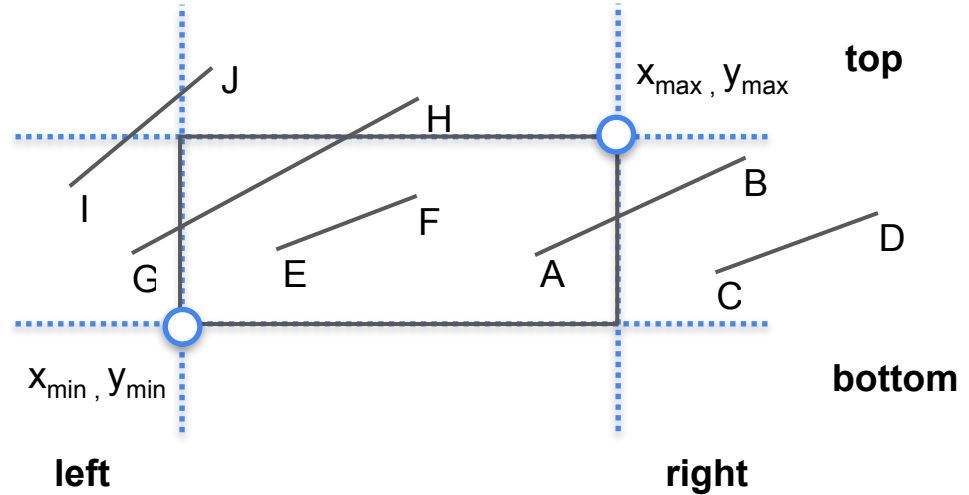
# Clipping: Cohen-Sutherland Line Clipping

	left	central	right
<b>top</b>	1001	1000	1010
$y_{max}$	<hr/>		
<b>central</b>	0001	0000	0010
$y_{min}$	<hr/>		
<b>bottom</b>	0101	0100	0110
	$x_{min}$	$x_{max}$	



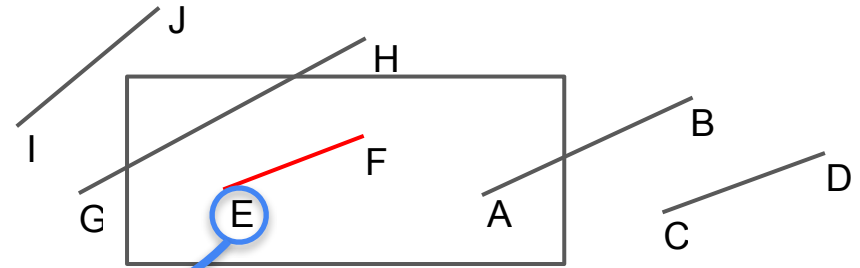
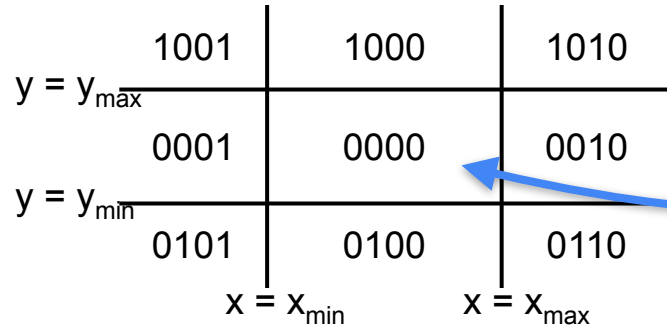
# Clipping: Cohen-Sutherland Line Clipping

```
outcode(x, y):  
    out = 0000    inside  
    if (y > ymax)  
        out = out | 1000    top  
    else if (y < ymin)  
        out = out | 0100    bottom  
    if (x > xmax)  
        out = out | 0010    right  
    else if (x < xmin)  
        out = out | 0001    left  
    return out
```



# Clipping: Cohen-Sutherland Line Clipping

Case 1: Trivial accept



$$o_1 = \text{outcode}(E_x, E_y) = 0000$$

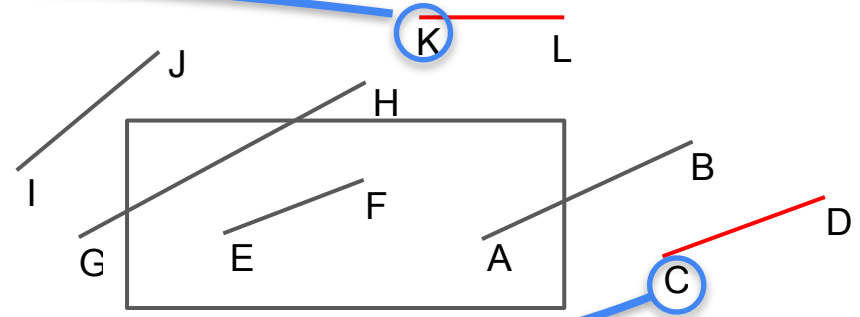
$$o_2 = \text{outcode}(F_x, F_y) = 0000$$

$$o_1 = o_2 = 0$$

# Clipping: Cohen-Sutherland Line Clipping

Case 2: Trivial reject

	1001	1000	1010
$y = y_{\max}$			
	0001	0000	0010
$y = y_{\min}$			
	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



$$o_1 = \text{outcode}(K_x, K_y) = 1000$$

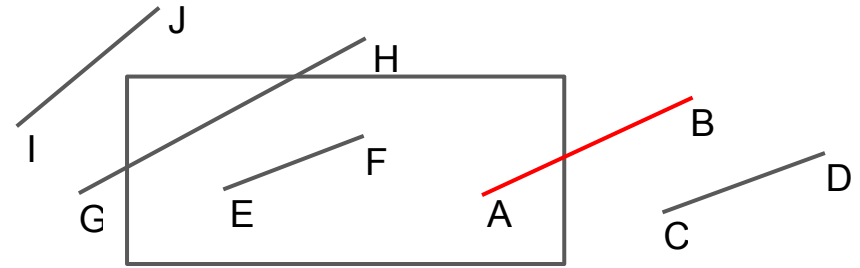
$$o_2 = \text{outcode}(L_x, L_y) = 1000$$

$$o_1 \ \& \ o_2 = 1000 \neq 0$$

# Clipping: Cohen-Sutherland Line Clipping

Case 3:

	1001	1000	1010
$y = y_{\max}$	-----		
	0001	0000	0010
$y = y_{\min}$	-----		
	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



$$o_1 = \text{outcode}(Ax, Ay) = 0000$$

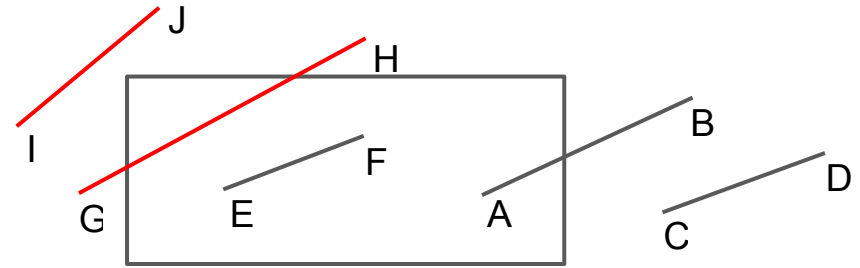
$$o_2 = \text{outcode}(Bx, By) = 0010$$

**$o_1 \neq 0$  and  $o_2 = 0$  or vice versa**

# Clipping: Cohen-Sutherland Line Clipping

Case 4:

	1001	1000	1010
$y = y_{\max}$	-----		
	0001	0000	0010
$y = y_{\min}$	-----		
	0101	0100	0110
	$x = x_{\min}$	$x = x_{\max}$	



$$o_1 = \text{outcode}(x_1, y_1)$$

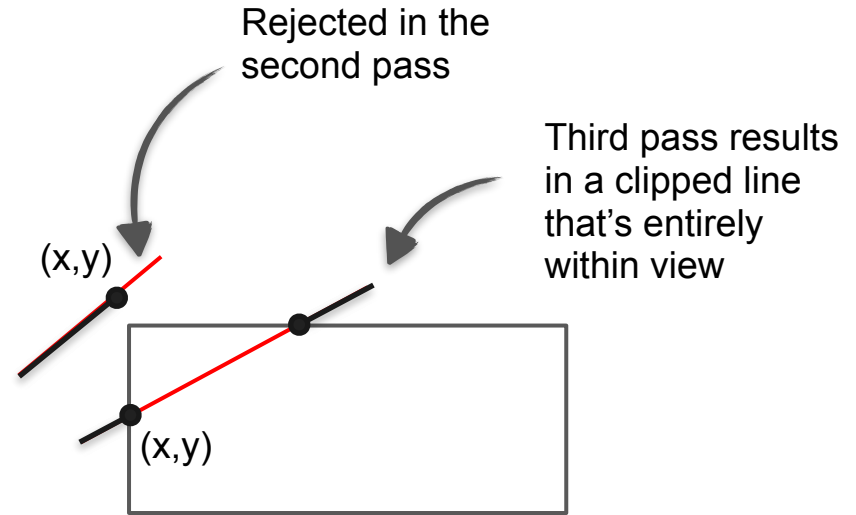
$$o_2 = \text{outcode}(x_2, y_2)$$

$$o_1 \& o_2 = 0$$

## Clipping: Cohen-Sutherland Line Clipping

### Intersection calculation:

- $y = mx + h$
- $m = (y_2 - y_1) / (x_2 - x_1)$
- $(y - y_1) = ((y_2 - y_1) / (x_2 - x_1)) * (x - x_1)$



### Disadvantages:

1. Algorithm is recursively applied (till the clipped result can be accepted or rejected).

# Clipping: Liang-Barsky Line Clipping

Algorithm makes use of parametric form of line.

Suppose:

$$P_1 = [x_1, y_1]^T \text{ and } P_2 = [x_2, y_2]^T.$$

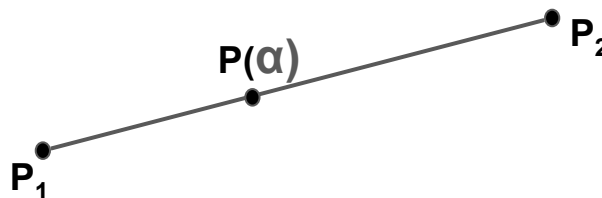
Then,

$$P(\alpha) = (1 - \alpha)P_1 + \alpha P_2$$

Or

$$x(\alpha) = (1 - \alpha)x_1 + \alpha x_2$$

$$y(\alpha) = (1 - \alpha)y_1 + \alpha y_2$$



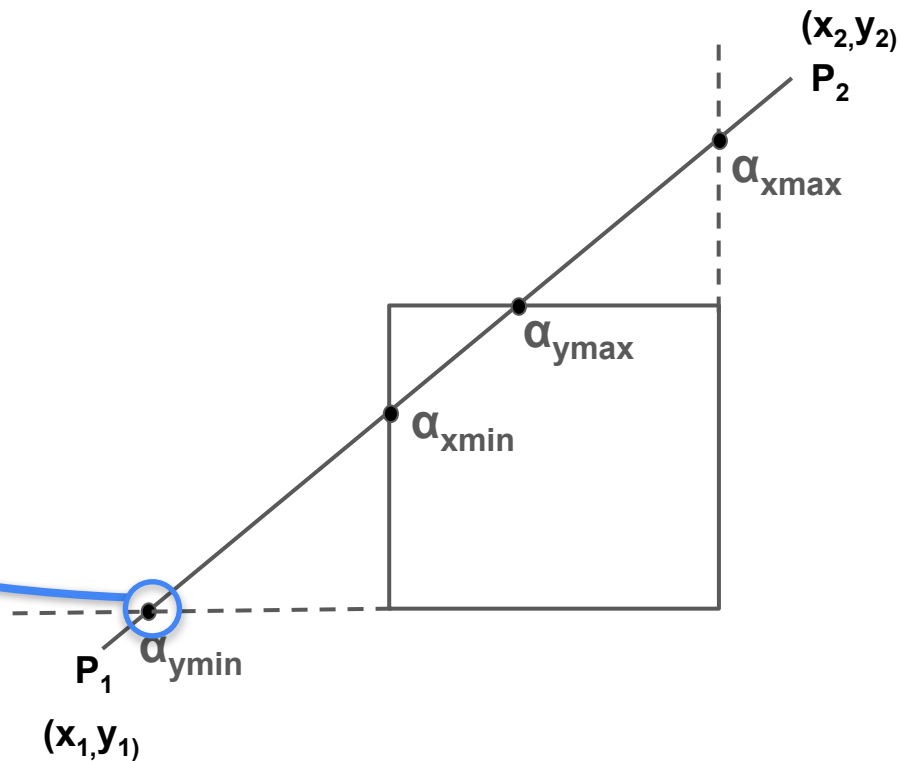
# Clipping: Liang-Barsky Line Clipping

Computing alpha values:

$$\alpha_{ymin} = (y_{min} - y_1) / (y_2 - y_1)$$

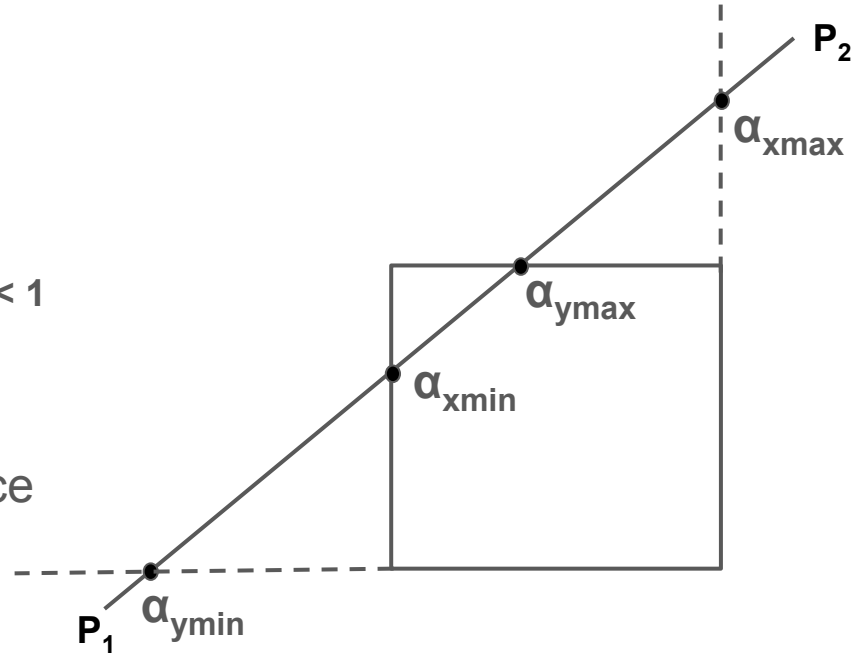
or

$$\Delta y \alpha_{ymin} = \Delta y_{min}$$



# Clipping: Liang-Barsky Line Clipping

- Compute the four  $\alpha$  values corresponding to four sides of the clipping window
- Compare them to find the order.
  - In this case  $0 < \alpha_{ymin} < \alpha_{xmin} < \alpha_{ymax} < \alpha_{xmax} < 1$
- Between two alpha values corresponding to vertical extremes if there is a horizontal alpha value (or vice versa) it indicates the line passes through the clip window.



# Clipping: Liang-Barsky Line Clipping

- Any  $\alpha$  value that is  $< 0$  or  $> 1$  implies the intersection happens on the extension of the actual line segment.

